

Making the Most of Predictive Models

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Outline

- 1 Introduction
- 2 Methodologies
 - Linear Methods
 - Nonlinear Methods
 - Feature Selection
- 3 Summary

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All Models Predict Something . . .

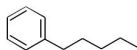
- Physics based models
 - Docking
 - Force fields
 - MD
- Statistical/ML models
 - Indirect description of the physical situation
 - Not always clear as to how a prediction is made

The Scope of Predictive Models

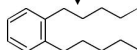
- Predictive models can be used for
 - filtering
 - analysis
- We can use predictive models in
 - chemometrics
 - bioinformatics
 - QSAR
 - ...
- What do we look for in a model?
 - Validity
 - Accuracy
 - Applicability
 - Interpretability

	Estimate	Std. Error	t value
(Intercept)	-1.635381	0.295587	-5.533
1	0.100694	0.037257	2.703
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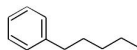


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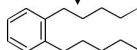
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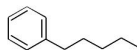


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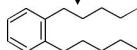
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Why Interpret a Model?

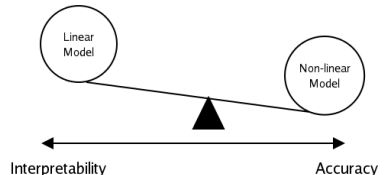
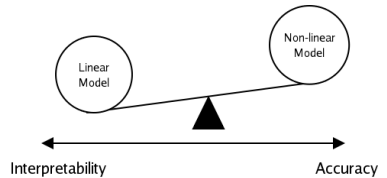
- A model encodes relationships between features and the property
- Understanding these relationships allows us to
 - understand why a molecule is active or not
 - suggest structural modifications
 - explain anomalous observations

How Much Detail Can We Extract?

- We can look at a model very broadly
 - Which descriptors are important to it's predictive ability?
- We can consider a more detailed analysis
 - What is the effect of descriptor X_i on \hat{Y}
 - Which observations highlight this relationship?
- Depends on how much effort you want to put in

The Accuracy - Interpretability Tradeoff

- OLS models are generally easier to interpret but not always accurate
- Neural networks give better accuracy, but are black boxes
- Some lie in between, such as random forests



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Model Types That We Can Interpret

- Depends on the
 - Level of interpretation desired
 - Nature of the problem (classification and regression)
- Some models are interpretable by design
 - Decision trees
 - Bayesian networks
- Other require an interpretation protocol
 - Linear regression
 - Random forests
 - Neural networks
 - Support vector machines

Guha, R.; Jurs, P.C., *J. Chem. Inf. Comput. Sci.*, **2004**, *44*, 2179–2189

Guha R. et al., *J. Chem. Inf. Model.*, **2005**, *46*, 321–333

Do, T.N.; Poulet, F., *Enhancing SVM with Visualization in Discovery Science*, Springer, **2004**, pp. 183–194

Linear Regression Interpretations

$$pK_a = -37.54Q_{\sigma,o} + 12.27A_{access,o} + 0.11\chi_{\pi,\alpha C} \\ -1.02\alpha_o - 1.89I_{amino} + 19.10$$

- Simply looking at the magnitude of the coefficients describes which descriptors are playing an important role
- Signs of the coefficients indicate the effect of the descriptor on the predicted property
- Interpretation is still quite broad
 - We'd like to see more detailed SAR's applied to individual molecules

Linear Regression Interpretations via PLS

- PLS overview
 - Creates a model with *latent variables*
 - Latent variables (components) are linear combinations of the original variables (X's)
 - Each latent variable is used to predict a *pseudo* dependent variable (Y's)
- Interpretation
 - The linear model is subjected to PLS analysis
 - This also *validates* the model
 - Choose the number of components to use
 - Interpretation uses the X-weights, X-scores & Y-scores

Linear Regression Interpretations via PLS

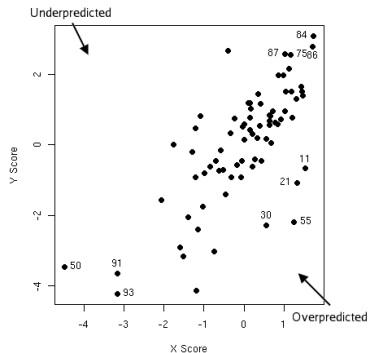
- Choosing components
 - Q^2 allows us to choose how many components
 - For a valid model cumulative variance should be 1
- Descriptor weights
 - Descriptors are ranked by their weights
 - Sign of weight indicates how the descriptor correlates to predicted activity

	X variance	R^2	Q^2
C1	0.51	0.52	0.45
C2	0.78	0.60	0.56
C3	1.00	0.61	0.56

Desc	C1	C2	C3
MDEN-23	-0.16	0.93	0.30
RNHS-3	0.55	-0.17	0.81
SURR-5	-0.82	-0.29	0.48

Linear Regression Interpretations via PLS

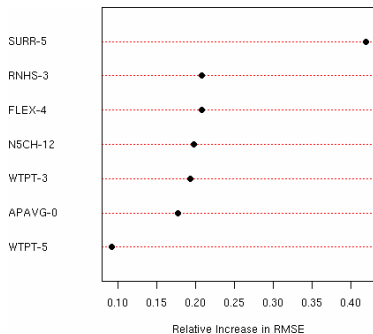
- Component 1
 - SURR-5 is most weighted
 - Low values of SURR-5 \Rightarrow high values of predicted activity
- Interpretation
 - Active compounds have high absolute values of SURR-5
 - Indicates large hydrophobic surface area
 - Consistent with cell based assay which depends on cell membrane transport



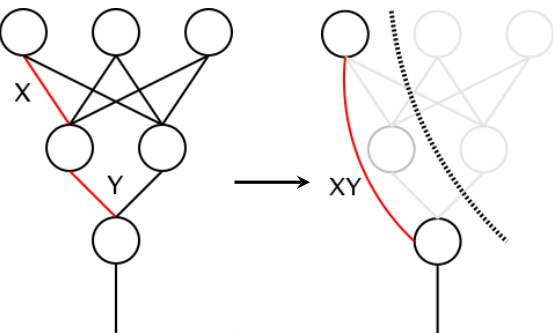
	MDEN-23	RNHS-3	SURR-5
C1	-0.16	0.55	-0.82

Random Forest Interpretations

- A RF provides a measure of descriptor importance
 - Utilizes the whole descriptor pool and ranks the descriptors
 - Based on randomization
- We can also get more information on individual trees
 - Find the most important trees
 - Consider a tree-space and find clusters of trees



Neural Network Interpretations



Effective Weight Matrix

Descriptor	Hidden Neuron	
	1	2
Desc 1	52.41	29.30
Desc 2	37.65	22.14
Desc 3	-10.50	-16.85

Linearizes the network and consequently loses some details of the encoded SAR's

Neural Network Interpretations

- The most weighted descriptors are very similar to those in the OLS model
- The signs of the effective weights match those from the OLS model as well as chemical reasoning

Descriptor	Hidden Neuron			
	1	3	2	4
PNSA-3	-1.80	-6.57	0.39	-1.43
RSHM-1	4.03	6.15	1.50	1.01
V4P-5	9.45	2.15	3.24	0.60
S4PC-12	3.36	2.73	1.99	0.56
MW	3.94	8.42	1.94	0.76
WTPT-2	1.71	2.61	1.17	-0.13
DPHS-1	0.66	0.44	0.33	1.65
SCV	0.52	0.33	0.13	0.01

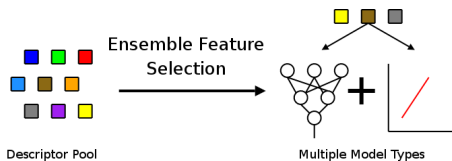
Size effects, higher
MW

H-bonding, HSA, polar
surface area

Stepping Back . . .

- We've been focusing on single model types
- Different models for different purposes
- Descriptors are optimal for a specific model
- Are we sure that the different models encode the same SAR's?

Getting the Best of Both Worlds



- Why not *force* multiple models to have the same descriptors?
 - The descriptor set will not be optimal for either model
 - Degradation in accuracy
- Is it really that bad?

Eating Our Cake . . .

- Ensemble feature selection
 - Select a descriptor subset that is *simultaneously* optimal for two different model types
- Allows us to build an OLS model and a CNN model using the same set of descriptors
- We use a genetic algorithm, where the objective function is of the form

$$RMSE_{OLS} + RMSE_{CNN}$$

We have one model for interpretability and one for accuracy, but they should now incorporate the same SAR's

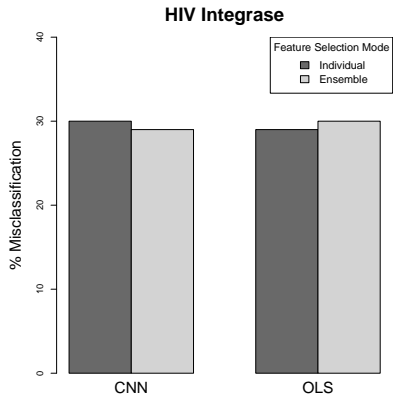
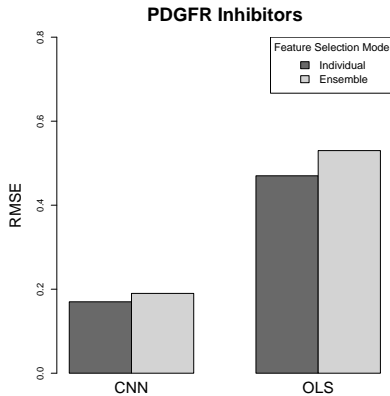
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...and Having it Too



Selecting for Interpretability

- Uptil now we've considered the models themselves
- But it's the descriptors we interpret
- Can we build models out of interpretable descriptors?
 - Design descriptors so that they have physical meaning
 - Exclude uninterpretable descriptors from the pool
 - Add semantic annotation to descriptors and modify feature selection algorithms to take this into account

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- Using models just for prediction is fine, but there's lots of extra information we can extract from them
- The extent of interpretability is guided by the nature of the problem, the choice of model and descriptors
- Interpretation of 2D-QSAR models allows us to get a little closer to the real physical problem

PLS Interpretation - Understanding Outliers

- Compound 55 is mispredicted by each component
- It is also an outlier in both linear & CNN models
- Has high absolute value of SURR-5 but low measured activity

