Navigating Molecular Haystacks: Tools & Applications Finding Interesting Molecules & Doing it Fast

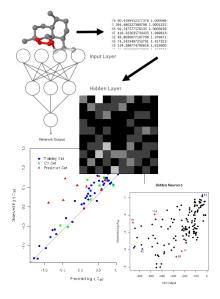
Rajarshi Guha

Department of Chemistry Pennsylvania State University

20st April, 2006

Past Work

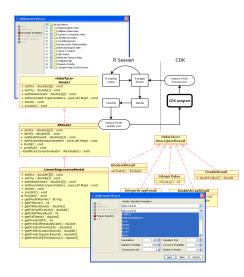
QSAR Applications • Artemisinin analogs PDGFR inhibitors • Bleaching agents • Linear & non-linear methods **QSAR** Methods Representative QSAR sets Model interpretation Model applicability



Past Work

Cheminformatics

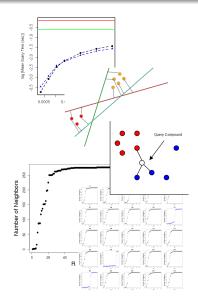
- Automated QSAR pipeline
- Contributions to the CDK
- Cheminformatics webservices
- R packages and snippets



Past Work

Chemical Data Mining

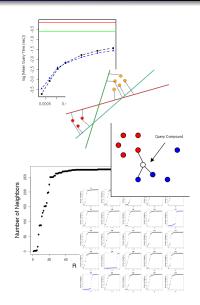
- Approximate k-NN
- Local regression
- Outlier detection
- VS protocol



Past Work

Chemical Data Mining

- Approximate k-NN
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Outline

- 1 Outlier Detection Using R-NN Curves
 - Methods for Diversity Analysis
 - Generating & Summarizing R-NN Curves
 - Using R-NN Curves
- 2 Searching for HIV Integrase Inhibitors
 - Previous Work on HIV Integrase
 - A Tiered Virtual Screening Protocol
 - What Does the Pipeline Give Us?

3 Summary

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Jsing *R*-NN Curves

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3 Summary

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Diversity Analysis

Why is it Important?

- Compound acquisition
- Lead hopping
- Knowledge of the distribution of compounds in a descriptor space may improve predictive models

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

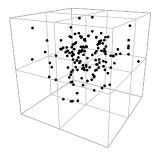
Approaches to Diversity Analysis

Cell based

- Divide space into bins
- Compounds are mapped to bins

Disadvantages

- Not useful for high dimensional data
- Choosing the bin size can be tricky



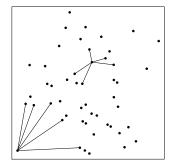
Schnur, D.; J. Chem. Inf. Comput. Sci. 1999, 39, 36–45 Agrafiotis, D.; Rassokhin, D.; J. Chem. Inf. Comput. Sci. 2002, 42, 117–12

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Approaches to Diversity Analysis

Distance based

- Considers distance between compounds in a space
- Generally requires pairwise distance calculation
- Can be sped up by *k*D trees, MVP trees etc.



Agrafiotis, D. K.; Lobanov, V. S.; J. Chem. Inf. Comput. Sci. 1999, 39, 51-58

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Generating an *R*-NN Curve

Observations

- Consider a query point with a hypersphere, of radius *R*, centered on it
- For small *R*, the hypersphere will contain very few or no neighbors
- For larger R, the number of neighbors will increase
- When $R \ge D_{max}$, the neighbor set is the whole dataset

The question is . . .

Does the variation of nearest neighbor count with radius allow us to characterize the location of a query point in a dataset?

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

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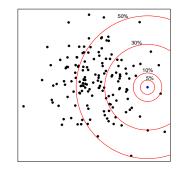
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Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Generating an *R*-NN Curve

Algorithm

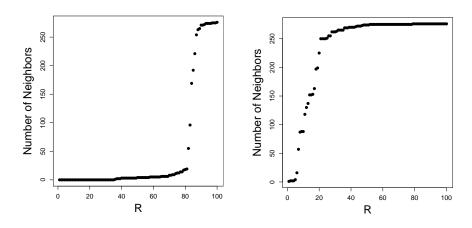
 $D_{max} \leftarrow \max$ pairwise distance for molecule *in* dataset do $R \leftarrow 0.01 \times D_{max}$ while $R \leq D_{max}$ do Find NN's within radius RIncrement Rend while end for Plot NN count vs. R



Guha, R.; Dutta, D.; Jurs, P.C.; Chen, T.; J. Chem. Inf. Model., submitted

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Generating an R-NN Curve



Sparse

Dense

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Characterizing an R-NN Curve

Converting the Plot to Numbers

• Since *R*-NN curves are sigmoidal, fit them to the logistic equation

$$N_N = a \cdot rac{1+m \ e^{-R/ au}}{1+n \ e^{-R/ au}}$$

- m, n should characterize the curve
- Problems
 - Two parameters
 - Non-linear fitting is dependent on the starting point
 - For some starting points, the fit does not converge and requires repetition

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

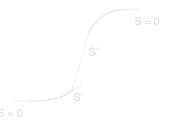
Characterizing an R-NN Curve

Converting the Plot to a Number

Determine the value of R where the lower tail transitions to the linear portion of the curve

Solution

- Determine the slope at various points on the curve
- Find *R* for the *first* occurence of the maximal slope (*R*_{max(S)})
- Can be achieved using a finite difference approach



Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

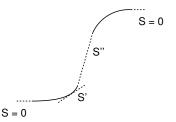
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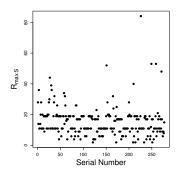
Characterizing Multiple R-NN Curves

Problem

- Visual inspection of curves is useful for a few molecules
- For larger datasets we need to summarize *R*-NN curves

Solution

- Plot $R_{max(S)}$ values for each molecule in the dataset
- Points at the top of the plot are located in the sparsest regions
- Points at the bottom are located in the densest regions



Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

How Can We Use It For Large Datasets?

Breaking the $O(n^2)$ barrier

- Traditional NN detection has a time complexity of $O(n^2)$
- Modern NN algorithms such as kD-trees
 - have lower time complexity
 - restricted to the exact NN problem

• Solution is to use *approximate NN* algorithms such as Locality Sensitive Hashing (LSH)

Bentley, J.; Commun. ACM 1980, 23, 214-229

Datar, M. et al.; SCG '04: Proc. 20th Symp. Comp. Geom.; ACM Press, 2004

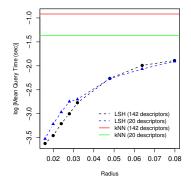
Dutta, D.; Guha, R.; Jurs, P.; Chen, T.; J. Chem. Inf. Model. 2006, 46, 321-333

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

How Can We Use It For Large Datasets?

Why LSH?

- Theoretically sublinear
- Shown to be 3 orders of magnitude faster than traditional kNN
- Very accurate (> 94%)



Comparison of NN detection speed on a 42,000 compound dataset using a 200 point query set

Dutta, D.; Guha, R.; Jurs, P.; Chen, T.; J. Chem. Inf. Model. 2006, 46, 321-333

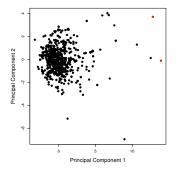
Alternatives?

Why not use PCA?

- *R*-NN curves are fundamentally a form of dimension reduction
- Principal Components Analysis is also a form of dimension reduction

Disadvantages

- Eigendecomposition via SVD is $O(n^3)$
- Difficult to visualize more than 2 or 3 PC's at the same time



Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Datasets

Boiling point dataset

- 277 molecules
- Average: MW = 115, $S_{tanimoto} = 0.20$
- Calculated 214 descriptors, reduced to 64

Kazius-AMES dataset

- 4337 molecules
- Average MW = 240, $S_{tanimoto} = 0.21$
- Known to have a number of significant outliers
- Calculated 142 MOE descriptors, reduced to 45

Goll, E.; Jurs, P.; J. Chem. Inf. Comput. Sci. **1999**, *39*, 974–983 Kazius, J.; McGuire, R.; Bursi, R.; J. Med. Chem. **2005**, *48*, 312–320

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Choosing a Descriptor Space

Boiling point dataset

- We had previously generated linear regression models using a GA to search for subsets
- Best model had 4 descriptors

Kazius-AMES dataset

- No models were generated for this dataset
- Considered random descriptor subsets
- Used a 5-descriptor subset to represent the results

The *R*-NN curve approach focuses on the distribution of molecules in a given descriptor space. Hence a *good* or *random* descriptor subset should be able to highlight the utility of the method

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

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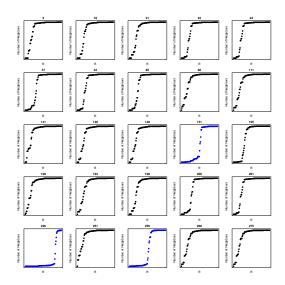
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Using R-NN Curves

R-NN Curves for the BP Dataset



Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Outliers for the Kazius-AMES Dataset

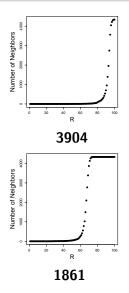
Defining outliers

•
$$R = 0.5 \times D_{max}$$

• NN count \leq 10% of the dataset

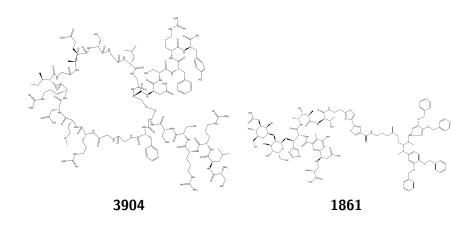
Outliers detected

- Molecule 3904 had 2 neighbors
- Molecule 1861 had 41 neighbors
- $R = 0.4 \times D_{max} \rightarrow 6$ outliers
- Clearly, this process is subjective



Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Outlier Structures

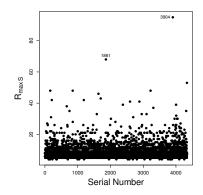


Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Summary of the Kazius-AMES Dataset

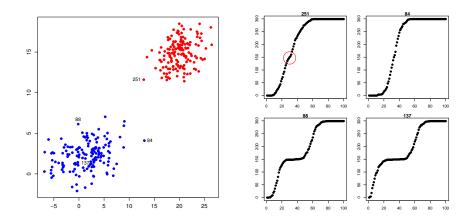
- **3904** & **1861** are immediately identifiable as outliers
- Excluding these two, there are no *significant* outliers
- The dataset appears to be relatively dense

One plot summarizes the location characteristics of *all* the molecules in the dataset



Using R-NN Curves

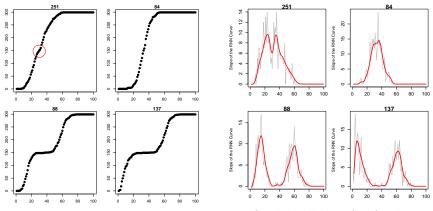
R-NN Curves & Clustering



Outlier Detection Using R-NN Curves

Searching for HIV Integrase Inhibitors Summary Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

R-NN Curves & Clustering



Smoothed with Friedmans Super Smoother

Friedman, J.H.; Laboratory for Computational Statistics, Stanford University, Technical Report 5, 1984

Methods for Diversity Analysis Generating & Summarizing *R*-NN Curves Using *R*-NN Curves

Conclusions

Future Work

- Allow comparison over multiple datasets
- Automated detection of clustering

Conclusions

- Applicable to arbitrary dimensions
- Can be easily extended to large datasets
- Summarizing a dataset does not require any user defined parameters
- Simple and intuitive approach to visualizing distribution of molecules in a descriptor space

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Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

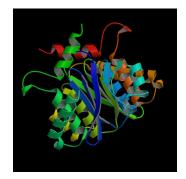
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 - Previous Work on HIV Integrase
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 - What Does the Pipeline Give Us?

3 Summary

Background

- Most drugs for HIV treatment target the protease or reverse transcriptase enzymes
- Integrase is essential for the replication of HIV
- There are no FDA approved drugs that target HIV integrase



Previous Work on HIV Integrase

1BIS

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Previous Work

Previous approaches

- Pharmacophore based models
- Docking

Disadvantages

- Requires a reliable receptor structure
- Computationally intensive
- Does not necessarily lead to a diverse hit list

Nair, V; Chi, G.; Neamati, N.; J. Med. Chem., 2006, 49, 445–447
 Dayam, R; Sanchez, T.; Neamati, N.; J. Med. Chem., 2005, 48, 8009–8015
 Deng, J. et al.; J. Med. Chem., 2005, 48, 1496–1505

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Goals

High speed

- Be able to process large libraries rapidly
- Avoid docking till required
- Try and use connectivity information only

Reliability

- Use a consensus approach for predictions
- Use molecular similarity to further prioritize predictions

Novelty

- Try to obtain hits suitable for lead hopping
- Try to obtain a diverse set of hits

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Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Datasets & Tools

Training data

- Curated dataset
- 529 inactives
- 395 actives
- Binary valued activity

Vendor database

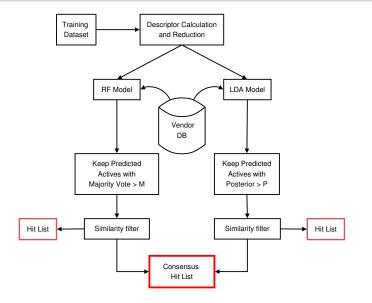
- 50,000 compounds
- 2D structures

Software

- MOE for descriptors
- R for the VS protocol
 - MASS
 - randomForest
 - fingerprint

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

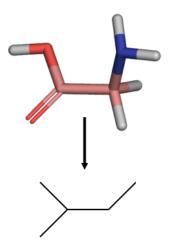
Overview of the Screening Protocol



Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Descriptor Calculations

- Restricted ourselves to topological & 2.5D descriptors
- 147 descriptors were evaluated
- Correlated and low variance descriptors were removed resulting in a reduced pool of 45 descriptors



Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Predictive Models - LDA

Why?

- Simple
- May be sufficient

How?

- Use a GA to search for good descriptor subsets
- Used a 6-descriptor model

Accuracy?

	Percent Correct
On whole dataset	72
On TSET/PSET	72 / 71
With leave-10%-out	71

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Predictive Models - Random Forest

Why?

- No feature selection required
- Does not overfit
- Useful for non-linearities in the dataset

How?

- Number of trees = 500
- Number of features sampled = 6

Accuracy

	Percent Correct
On whole dataset	72
On TSET/PSET	75 / 70

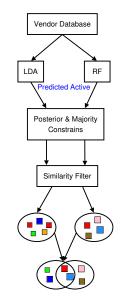
Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Consensus Predictions

Goal

Try and be sure that a predicted active is active

- Consider compounds predicted active by *both* models
 - LDA: consider compounds with posterior > P
 - RF: consider compounds with majority vote > M
- Apply similarity filter
- We now have 2 hit lists
- A final hit list is obtained from the intersection of the individual hitlists



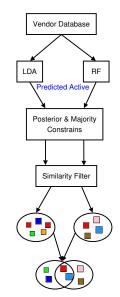
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Similarity Filter

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Goal

Predict actives from vendor database that are more similar to actives than inactives

- Evaluate 166 bit MACCS fingerprints
- Evaluate average Tanimoto similarity between
 - Vendor compound and TSET actives (S_1)
 - Vendor compound and TSET inactives (S₂)
- Select compounds where

$$S_1 - S_2 \ge \epsilon$$

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A Tiered Virtual Screening Protocol

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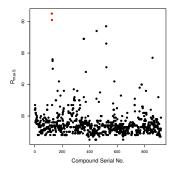
$$S_1 - S_2 \ge \epsilon$$

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Suggesting Good Leads

Can we prioritize further?

- Look for TSET actives that are outliers
- These compounds may be good starting points for further modifications
- Evaluate similarity of hit list compounds to these isolated TSET compounds
- Hit list compounds most similar to the most isolated TSET active may be good leads



The points marked red are the most outlying compounds in the TSET and are also active

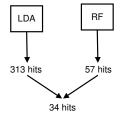
Saeh, J.C.; Lyne, P.D.; Takasaki, B.K.; Cosgrove, D.A.; J. Chem. Inf. Comput. Sci., 2005, 45, 1122-1133 Guha, R.; Dutta, D.; Jurs, P.C.; Chen, T; J. Chem. Inf. Model., submitted

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Results

Summary of the hits

- Parameter settings
 - *P*, *M* > 0.7
 - $\epsilon \geq 0.01$
- Of the 34 hits, 7 had a similarity > 0.5 with the most outlying TSET active
- We obtained 66 more hits from an ensemble of LDA models

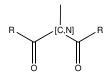


- Average similarity = 0.64
- Not significantly diverse
- None were in common with those predicted by the pharmacophore models

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

The Search for β -diketones

- A recently published inhibitor exhibited a β -diketone moiety
- None of our hits had this moiety



• Searched the vendor DB for structures with this feature and predicted them

- LDA model \rightarrow 244 actives (posterior > 0.8)
- RF model \rightarrow 4 actives (score > 0.85)
- The intersection set contained 4 compounds

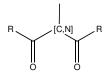
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Nair, V; Chi, G.; Neamati, N.; J. Med. Chem., 2006, 49, 445-447

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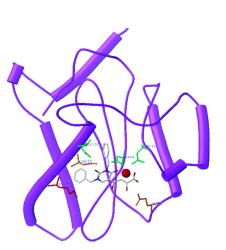


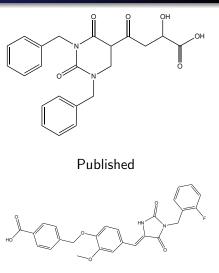
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Nair, V; Chi, G.; Neamati, N.; J. Med. Chem., 2006, 49, 445-447

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Similarity to the Published Compound





Predicted

Nair, V; Chi, G.; Neamati, N.; J. Med. Chem., 2006, 49, 445-447

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

Future Work

Reliability

- Consider similarity to known actives in terms of pharmacophores
- Dock our best hits (may not be conclusive)
- Improve performance with *local* methods

Diversity

- Investigate distribution of vendor compounds in the descriptor space
- Cluster the vendor DB and predict representative members of the clusters

Previous Work on HIV Integrase A Tiered Virtual Screening Protocol What Does the Pipeline Give Us?

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Assay!

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3 Summary

Summary

- The outlier detection scheme provides a way to analyze spatial distributions of molecules in arbitrary descriptor spaces
- The method can be extended to large datasets using approximate NN algorithms
- The technique results in a single intuitive plot that can be used to easily identify outliers
- A consensus approach to predictive models allows us to increase confidence in activity predictions
- Prioritization based on similarity is intuitive, but may not work well with homogenous datasets
- The protocol appears to have identified possible leads which await confirmation

Summary

- The outlier detection scheme provides a way to analyze spatial distributions of molecules in arbitrary descriptor spaces
- The method can be extended to large datasets using approximate NN algorithms
- The technique results in a single intuitive plot that can be used to easily identify outliers
- A consensus approach to predictive models allows us to increase confidence in activity predictions
- Prioritization based on similarity is intuitive, but may not work well with homogenous datasets
- The protocol appears to have identified possible leads which await confirmation

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- Prof. P. C. Jurs
- Dr. D. Dutta
- Prof. N. Neamati
- Dr. R. Dayam

Why are *R*-NN Curves Sigmoidal?

- Let the neighbor density be ρ_0
- At some critical radius, r_0 , the neighbor density changes to $\rho_1, \ \rho_1 >> \rho_0$
- After a certain radius, *R*, the number of NN's becomes constant, *N*
- For a radius $r < r_0$, consider a small change dr
- The number of NN's on the strip is $2\pi\rho_0 dr$ which on integration gives $2\pi\rho_0 r_0^2$

Why are *R*-NN Curves Sigmoidal?

- Let the neighbor density be ρ_0
- At some critical radius, r₀, the neighbor density changes to ρ₁, ρ₁ >> ρ₀
- After a certain radius, *R*, the number of NN's becomes constant, *N*
- For a radius $r < r_0$, consider a small change dr
- The number of NN's on the strip is $2\pi\rho_0 dr$ which on integration gives $2\pi\rho_0 r_0^2$

Why are *R*-NN Curves Sigmoidal?

• For a radius $r_0 < r < R$, the number of NN's is given by

$$2\pi\rho_0 r_0^2 + \int_{r_0}^r 2\pi r \rho_1 dr$$

• The number of nearest neighbors as a function of r is

$$NN(r) = \begin{cases} 0 & \text{if } r \le 0\\ 2\pi\rho_0 r^2 & \text{if } 0 < r \le r_0\\ 2\pi\rho_0 r_0^2 + 2\pi\rho_1 (r^2 - r_0^2) & \text{if } r_0 < r < R\\ N & \text{if } r \ge R \end{cases}$$

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Zhang, M.; Vassiliadis, S.; Delgado-Frias, J.; IEEE Trans. Comput., 1996, 45, 1045-1049

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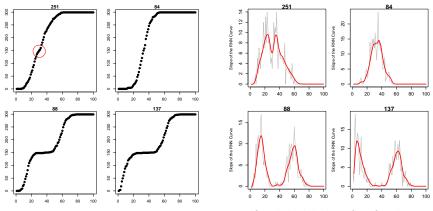
Zhang, M.; Vassiliadis, S.; Delgado-Frias, J.; IEEE Trans. Comput., 1996, 45, 1045-1049

R-NN Curves & Clustering

How Do We Characterize Curves?

- 🗴 RMSE
- X Generating a mean curve
- Examine slopes
- Piecewise linear approximation
- Compare distance matrices
- Shape matching
 - Hausdorff distance
 - Fréchet distance

R-NN Curves & Clustering



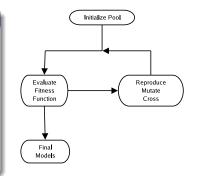
Smoothed with Friedmans Super Smoother

Friedman, J.H.; Laboratory for Computational Statistics, Stanford University, Technical Report 5, 1984

Genetic Algorithms

Features

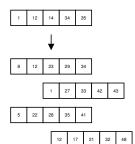
- Stochastic optimization procedure
- Based on evolutionary principles
- Applicable to large search spaces
- Not always guaranteed to find the optimal solution
- Fitness is evaluated by the *objective function*



Genetic Algorithms

Initialization

- Initially random chromosomes
- Chromosome length is the size of the descriptor subset
- Genes are the descriptors
- Larger pool sizes allow for a wider search

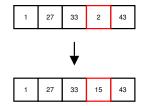


Summary

Genetic Algorithms

Mutation

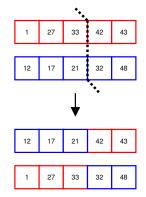
- Mutation frequency is relatively low
- Mutations randomly change a single descriptor
- Helps to get out of local minima



Genetic Algorithms

Crossover

- Crossover results in swapping of genes
- Crossover between fit individuals should lead to children with good aspects of both parents
- In single point crossover
 - Choose crosspoint
 - Swap corresponding sections
 - Results in two new children



Random Forest

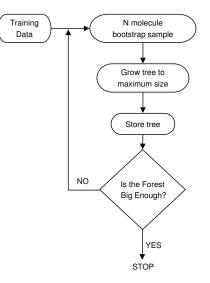
Features

- Built in estimation of prediction accuracy
- Measure of descriptor importance
- Measure of similarity

Random Forest vs. Decision Tree

- RF is faster because it searches fewer descriptors at each split
- A decision tree must be pruned via cross validation. RF trees are grown to full depth
- RF is much more accurate than a decision tree

Random Forest



OOB Samples

What is OOB?

- Due to bootstrap sampling, each tree uses pprox 2/3 of the TSET
- The remaining 1/3 is the Out Of Bag sample
- The OOB sample can be used to estimate performance during training or measure descriptor importance

Descriptor Importance

- Decision trees create explicit relationships between descriptors and predictions
- These relationships are hidden in a RF model
- A randomization procedure on OOB samples can be used to rank descriptors in importance

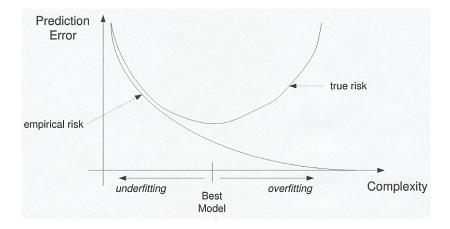
Model Complexity

- Very simple models or very complex models may perform poorly
- The optimal performance and complexity are obtained from a trade off between *bias* and *variance*

Mean Squared Error = $Var(\hat{y}) + Bias^2(\hat{y})$, where

$$\textit{Var} \propto \frac{1}{\textit{complexity}}$$
 and $\textit{Bias} \propto \textit{complexity}$

Model Complexity



http://www.ece.wisc.edu/~nowak/ece901/lecture3.pdf